# Pattern-Driven Navigation in 2D Multiscale Visualizations with Scalable Insets

## **Supplementary Material**

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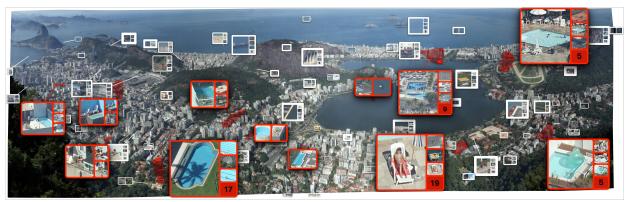
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## **Supplementary Figures**

## 1. Overview



# 2. Frequently Annotated Pattern Types



# 3. Unexpected Patterns



Figure S1: Scaled-up version of Figure 3.1-3

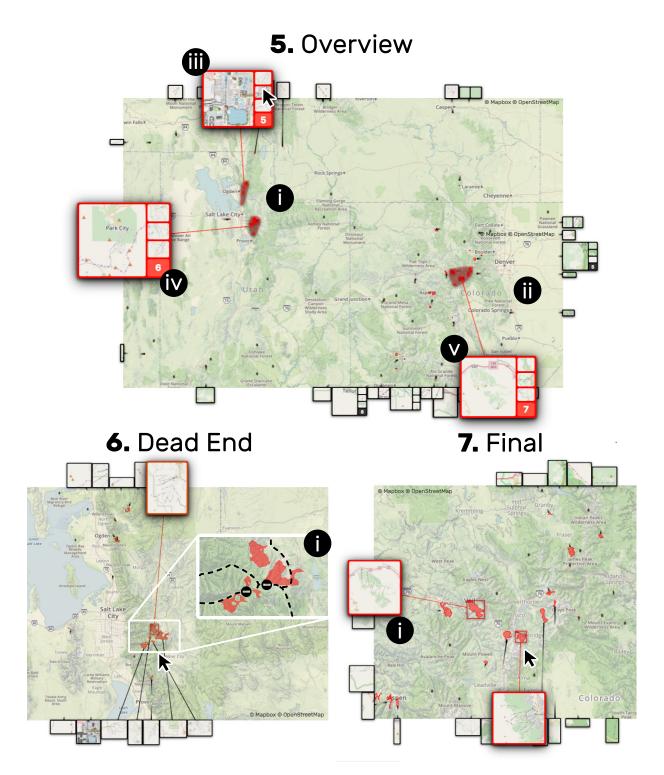


Figure S2: Scaled-up version of Figure 3.5-7

### Key points of the Animation

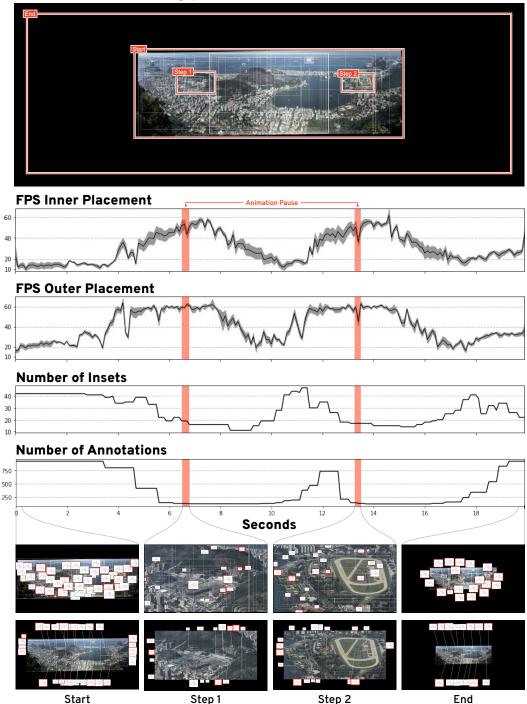


Figure S3: Detailed view of the performance analysis explained in Section 6.3. The gray area in "FPS Inner Placement" and "FPS Outer Placement" shows the standard error. The two regions highlighted in red mark 250-millisecond pauses of the animated transition between the key points. For static views Google Chrome's DevTool v74 reports very low frame rates as the frames are not refreshed. Therefore the FPS during these two pauses should be ignored.

### Data Visualization Closing Questionnaire

First of all: thank you for participating in our user study. 🌂 Please tell us your email one more time. We need it to send you the compensation in form of an Amazon gift card.

\* Required

#### Email address \*

Your email

#### Terminology

SUBMIT

Never submit passwords through Google Forms.

In the following we refer to the small magnified thumbnails as insets.

What is your overall impression of the inset techniques?

,							
		1	2	3	4	5	
not impressive		0	0	0	0	$\bigcirc$	very impressive
		•					nd aggregated inding interesting
	1	2		3	4	5	
disagree	0	0		0	0	$\circ$	strongly agree
How easy wa	as it to	o learn	the	interf	ace fo	or the in	set techniques?
		1	2	3	2	ц 5	
very unintuitive		0	0	С	$\sim$	C	) very intuitive
Are there any parts of the interface that were not intuitive?							
Your answer							
Is there anything else you want to tell us?							
Your answer							
Thanks so m	uch a	again f	or yo	our he	lp! 👍	You're	the best! 🎉

Figure S4: A screenshot of the closing questionnaire of user study 1 for completeness. The questionnaire was realized with Google Forms. The results are presented in Table S2.

### **Supplementary Tables**

Component	Weight	Unit	Normalized By	Formula
inset distance	1.0	pixels	inset radius	$\ i^c - s^c_i\ /r^i$
inset-inset overlap	2.0	pixels <sup>2</sup>	inset area	$\operatorname{overlap}(i, j) / \min(i^a, j^a)$
inset-source overlap	2.0	pixels <sup>2</sup>	source area	$\operatorname{overlap}(i, s_i)/s_i^a$
inset-annotation overlap	0.5	pixels <sup>2</sup>	annotation area	$\operatorname{overlap}(i,a)/a^a$
inset-inset min. distance	0.5	pixels	inset radius	$\max(0, (r_i -   i^c - j^c  )/r_i)$
inset-source min. distance	0.5	pixels	inset radius	$\max(0, (r_i - \ i^c - s_i^c\ )/r_i)$
inset-annotation min. distance	0.25	pixels	inset radius	$\max(0, (r_i + b_a - \ i^c - a^c\ )/r_i)$
leader line intersection	1.0	count	none	intersect(i, j)
move distance	0.5	pixels	inset radius	$  m_i  /r^i$

Table S1: Components with their default weights and normalization terms. The notation follows Section 4, where *i* and *j* represent two insets. Additionally,  $i^c$ ,  $s^c$ , and  $a^c$  stand for the location of the center of an inset, an inset's source annotation, or another annotation. The area of an annotation is denoted by  $s^a$  or  $a^a$  and the breadth an annotation is denoted by  $b_a$ . We differentiate between "sources" and "annotations", where "sources" are annotations too small to be identifiable and are associated with insets and "annotations" are all other annotations that are large enough to be considered identifiable. The inset radius  $r_i$  is defined as  $\sqrt{(0.5 \times width)^2 + (0.5 \times height)^2}$ .

1	2	3	4	5				
1. What is your overa	1. What is your overall impression of the inset techniques? (1: not impressive; 5: very impressive)							
		XXXXX	XXXXXXXXXX	XXX				
2. Do you think the c	2. Do you think the concept of previewing small and aggregated regions as insets within the view is							
helpful for finding int	teresting regions? (1: d	isagree; 5: strongly agr	ee)					
	Х	XXXX	XXXXXXXXXX	XXX				
3. How easy was it to intuitive)	b learn the interface for	the inset techniques?	(1: very unintuitive; 5:	very				
	X	XX	XX	XXXXXXXXXXXX				
4. Are there any parts	s of the interface that w	ere not intuitive?						
<ul> <li>Make aggregat</li> <li>Foreign termin</li> <li>Enlarge insets</li> <li>Inset movemen</li> <li>Insets were ver</li> <li>Difference bet</li> </ul>	<ul> <li>Manually show an inset through a click on the bounding box of the source annotation</li> <li>Pile size number is confusing as it's not always visible</li> <li>Make aggregated insets dispersable</li> <li>Foreign terminology (copula)</li> <li>Enlarge insets on zoom (i.e., the mouse wheel event)</li> <li>Inset movement was distracting (inner-placement)</li> <li>Insets were very prominent</li> <li>Difference between cluster representatives is not obvious</li> </ul>							
5. Is there anything e	lse you want to tell us?							
Scroll acceleration	eeds to be taken into ac	ccount						

Table S2: Closing questionnaire of the first user study. Each "x" stands for the answer of one of the participants. The lists for question 4 and 5 have been paraphrased and combined for brevity. The questionnaire was realized with Google Forms and translated into this table. For completeness please see a screenshot of the Google Form in Figure S4. The wording and values are identical. We employed end labeling, i.e., only points 1 and 5 were labeled as shown above. All questions were optional.

Participant	Action							
P1	Started with inner-placement							
	• Slow panning to gain an understanding of the view and data							
	• Gently zoomed to an inset to investigate the context							
	Panned along the diagonal							
	• Scaled up and down a cluster of two insets to quickly investigate the visual struc							
	ture of the patterns							
	<ul> <li>Continued panning to search for patterns</li> </ul>							
	Switched to outer-placement view							
	<ul> <li>Zoomed out</li> </ul>							
	Identified new pattern type							
	• Assessed the original location of the new pattern type through hovering the inset							
	• Panned to another region							
	• Investigated the appearance and disappearance of insets based on the zoom level							
	• Scaled up an inset showing a different pattern type							
P2	Started with inner-placement							
	<ul> <li>Obtained an overview through brief zoom out</li> </ul>							
	• Zoomed back in to initial zoom level							
	• Dragged an aggregate of insets away to study context							
	• Rapidly panned down the diagonal of the matrix to find dot-like patterns							
	• Dragged a pile of insets away to study context							
	• Scaled up and leafed through a pile of insets							
	• Down scaled a pile of insets as no dot-like patterns were found							
	<ul> <li>Zoomed out and panned further to gain a better overview</li> </ul>							
	<ul> <li>Found a pile of two insets at the corner of a large square-like, annotated pattern</li> </ul>							
	<ul> <li>Zoomed in to the cluster to inspect the neighborhood of the insets</li> </ul>							
	<ul> <li>Zoomed out again and kept on panning</li> </ul>							
	• Encountered slowness due to a large amount of data loading							
	• Leafed through a large pile and found some dot-like pattern							
	• Zoomed into location to explore the local neighborhood							
	Switched to outer-placement view							
	• Scaled up all the piles of insets to search for dot-like-patterns							
	<ul> <li>Found one instance and zoomed in to that location</li> </ul>							
	<ul> <li>Rapidly panned to other location while searching for dot-like patterns</li> </ul>							
	Loaded square-like patterns							
	• Explored and found a square-like pattern							
	• Zoomed in and out investigated the loss of inset							
	• Zoomed all the way out to look that the square-like patterns globally							
	• Scaled up and leafed through several piles of insets with unexpected variances							
23	Started with inner-placement							
5	<ul> <li>Obtained an overview through gentle panning and zooming</li> </ul>							
	<ul> <li>Adjusted color map of the matrix</li> <li>Zoomed out to gain a broader overview</li> </ul>							
	<ul> <li>Zoomed out to gain a broader overview</li> <li>Zoomed hook in to study dataila</li> </ul>							
	• Zoomed back in to study details							
	• Dragged a pile of insets to see the nearby context							
	• Zoomed in to the location containing the insets of the pile							
	• Zoomed out a bit and panned to other locations							

#### Switched to outer-placement view

- Zoomed out a bit and panned to other locations
- Investigated disappearance of an inset
- Panned to another location
- Scaled up a square-like pattern and investigated the detailed visual structure in the inset
- Zoomed out while keeping the inset scaled up.
- Scaled up another cluster of insets with square-like patterns
- Leafed through the cluster to investigate the insets individually as the patterns show some expected details
- Panned to another location
- Scaled up an inset but kept on panning

Started	with	inner-placement	
---------	------	-----------------	--

- Panned rapidly down the diagonal
- Zoomed out to get a broader overview
- Zoomed back in a bit

P4

P5

- Dragged a pile of insets away to assess the occluded context
- Continued panning to find a dot-like pattern
- Scaled up an inset with a dot-like pattern
- Zoomed in to the location of the dot-like pattern
- Zoomed out to perceive the context at a lower resolution

Switched to outer-placement view

- Moved the mouse cursor over the insets to assess their original location
- Zoomed and panned a bit
- Tried to combine two insets into a pile
- Reset the location of the insets
- Scaled up one inset to look at the detailed visual structure
- Zoomed into the origin of the scaled-up inset
- Investigated when insets disappear
- Panned and zoomed further
- Zoomed out and compared to distant insets by dragged them next to each other
- Zoomed out further out to gain a broader overview

Started with inner-placement

• Started panning

• Identified a specific pattern in an inset and zoomed into the inset's original location

- Zoomed out and panned to another location
- Found an unexpected pile of insets with "empty" patterns
- Zoomed in a bit and confirmed their hypothesis
- Zoomed out and found another inset with an expected pattern
- Zoomed in to the inset's original location to study the context
- Zoomed out and compared the inset to other close-by insets

Switched to outer-placement view

• Scaled up a pile of insets to investigate the detailed visual structure of a squarelike pattern

- Leafed through the pile of insets
- Zoomed into the original location of the pile of insets

P6	Started with outer-placement					
	• Gently panned and zoomed to gain an overview					
	• Zoomed in to see more details					
	• Scaled up two insets consecutively					
	• Tried to zoom into the location of an inset via a double click					
	• Zoomed in to the inset's original location using the context menu					
	• Zoomed out again after investigating the context of the annotated pattern					
	Panned to another location					
	• Scaled up an inset with a square-like pattern					
	Switched to outer-placement view					
	• Zoomed in and out to understand the new placement behavior					
	• Zoomed all the way out to find long-distant patterns, i.e., patterns far away from					
	the diagonal of the matrix					
	• Zoomed in to a region without insets					
	• Panned elsewhere along the diagonal					
	• Scaled up an inset showing an unexpected pattern					
	• Zoomed into the inset's original location but stopped half-way to investigate another inset					
	• Panned to another region in the matrix					
	• Closely investigated the detailed visual structure of three insets consecutively					
	ronological summary of participant-specific actions and related tasks of the second, qualitative the domain experts.					

1	2	3	4	5				
1. What is your overall i	impression of the navig	ation technique? (1: no	ot impressive; 5: very in	mpres-				
sive)		-		-				
		Х	XXX	XX				
2. Do you think the con-	cept of previewing sma	all and aggregated region	ons as insets within the	view				
is useful for finding inte	resting regions, i.e., do	es it shorten the time to	decide if we region is	worth				
exploring in detail? (1: c	lisagree; 5: strongly ag	ree)						
			XX	XXXX				
3. How intuitive is the ir	nterface? (1: very unint	uitive; 5: very intuitive)	)					
	X		XXXX	X				
4. Are there any parts of	the interface that were	not intuitive?						
<ul> <li>Re-sync button no</li> <li>Border gallery</li> <li>Fading lines are c</li> <li>Pile aggregation t</li> </ul>	<ul> <li>With a very brief introduction (&lt;5min) things were understandable</li> <li>Re-sync button not obvious</li> <li>Border gallery</li> <li>Fading lines are confusing</li> <li>Pile aggregation type not obvious</li> <li>Disappearance of snippets is confusing</li> </ul>							
5. How useful is the tool	l in its current form to y	ou? (1: not useful at al	l; 5: very useful)					
	x	xx	xx	x				
6. Is this kind of explora	ation currently possible	in any other form? (1:	not at all; 5: very sim	ilar				
tools exist)		-	-					
XXX	X	XX						
7. If so, how does our to	ool compare against the	other methods in term	s of performance (A) a	and				
features (B)? (1: worse;	5: much better)		n					
A x	X		Х					
В	X	X	X					
8. Which (navigation) for sort by importance)	eatures (if any) are mis	sing that would make the	his tool more useful? (	Please				
<ul> <li>User-resizable snippets (2x)</li> <li>Change color scale</li> <li>Scale bar for snippet size</li> <li>Delete snippets</li> <li>Add new snippets manually (2x)</li> <li>Toggle between placing techniques</li> <li>Pin snippets</li> <li>Adjust aggregate representation</li> <li>Filter displayed snippets by some value</li> </ul> 9. Imagine all missing features are implemented, how useful would do you think would this tool be								
			you think would this t	tool be				
to the research communi	ity? (1: not useful at all	; 5: very useful)	1	1				
10 0 11		1 11	XX	XXXX				
10. Could you imagine graphic maps, large imag				geo-				
			Х	XXXXX				

Table S4: Closing questionnaire of the second user study. Each "x" stands for the answer of one of the six participants. The lists for question 4 and 8 have been paraphrased and combined for brevity. We employed end labeling, i.e., only points 1 and 5 were labeled as shown above. All questions were optional.

Parameter	INSIDE	OUTSIDE					
insets.labelPosition	hidden						
insets.minSize	:	32					
insets.maxSize	56						
insets.sizeStepSize	2						
insets.scale		1					
insets.scaleSizeBy	s	ize					
insets.additionalZoom		1					
insets.onClickScale		3					
insets.fill	wh	ite					
insets.fillOpacity		1					
insets.borderColor	wh	ite					
insets.borderWidth		1					
insets.borderOpacity		1					
insets.borderRadius		4					
insets.leaderLineColor	wh	ite					
insets.leaderLineWidth		2					
insets.leaderLineOpacity		1					
insets.leaderLineStubWidthMin		2					
insets.leaderLineStubWidthMax		4					
insets.leaderLineStubLength		12					
insets.leaderLineDynamic		true					
insets.leaderLineDynamicMinDist		24					
insets.leaderLineDynamicMaxDist		120					
insets.dropDistance	1						
insets.dropBlur	3						
insets.dropOpacity	C	0.8					
insets.opacity	1						
insets.showClusterSize	t:	rue					
insets.isDraggingEnabled	true	false					
insets.loadHiResOnScaleUp	t:	rue					
insets.isImgSelectable	false for PATTER	N and true for TYPE					
meta.insetThreshold	:	12					
meta.gridSize	72	52					
meta.minClusterSize		3					
meta.maxClusterDiameter	96	64					
meta.boostContext	1	0					
meta.boostDetails	1	10					
meta.boostLocality	1	1					
meta.boostLayout	1	5					
meta.cooling		1					
meta.reheat	0	.05					

Table S5: Parameter settings for INSIDE and OUTSIDE of the controlled user study with gigapixel images. The settings prefixed with "insets" refer to Insets2dTrack and the settings prefixed with "meta" refer to AnnotationsToInsetsMetaTrack. See https://github.com/flekschas/ higlass-scalable-insets for more information. Table S6: Aggregation of the absolute votes from the closing questionnaires (Table S2 and S4). Mean values are shaded by their values. \*Note that Q3 of study 1 was answered by 17 out of 18 and Q7 of study 2 was answered by 3 out of 6 participants only. Regarding the latter two, the *missing* votes are due to the fact that 3 participants for Q6 voted that no other tool currently supports exploration like Scalable Insets and, hence, did not have to answer Q7.

		Study 1			Study 2							
	Q1	Q2	Q3*	Q1	Q2	Q3	Q5	Q6	Q7A*	Q7B*	Q9	Q10
Mean	3.9	3.8	4.5	4.2	4.7	3.7	3.5	1.8	2.3	3.0	4.7	4.8
1, 2, and 3	5	5	3	1	0	1	3	6	2	2	0	0
4 and 5	13	13	14	5	6	5	3	0	1	1	6	6

Table S7: Technical setup of both user studies

Computer	Apple MacBook Pro 2016
Processor	Intel 2.7 GHz quad-core
Memory	16 GB
Display	15"
Effective resolution	$1440 \times 900$ pixels
<b>Operating system</b>	macOS 10.12
Input device	Standard two-button mouse with a scroll wheel

### **Supplementary Pseudo Code**

```
input :insets I, maximum inset size size, view height height, and view width width
```

```
1 numBinsX \leftarrow |width/size|;
 2 numBinsY \leftarrow |height/size|;
 3 binsLeft = binsRight = list of length numBinsY;
 4 binsTop = binsBottom = list of length numBinsX;
5 for inset i \in I do
       BinX \leftarrow |i.x/(width/numBinsX)|;
 6
       BinY \leftarrow |i.y/(height/numBinsY)|;
 7
       dLeft \leftarrow i.x + GetBinValue(binsLeft, BinY) * size;
 8
       dRight \leftarrow width - i.x + GetBinValue(binsRight, BinY)|) * size;
 9
       dTop \leftarrow i.y + GetBinValue(binsTop, BinX) * size;
10
11
       dBottom \leftarrow height -i.y + GetBinValue(binsBottom, BinX) * size;
       closestSide \leftarrow i.side or GetClosestSide (dLeft, dRight, dTop, dBottom);
12
       switch closestSide do
13
           case left do
14
               i.side \leftarrow left;
15
               IncrementBinValue (binsLeft, BinY));
16
17
           end
           case right do
18
               i.side \leftarrow right;
19
               IncrementBinValue (binsRight, BinY));
20
           end
21
           case top do
22
23
               i.side \leftarrow top;
               IncrementBinValue (binsTop, BinX));
24
           end
25
           case bottom do
26
               i.side \leftarrow bottom:
27
               IncrementBinValue (binsBottom, BinX));
28
           end
29
       end
30
31 end
```

Algorithm S1: Gallery Layout: Assign Insets to a Side. Insets are initially assigned to the closest side with the fewest number of insets already assigned to the bin of the corresponding x or y screen location of the inset. Upon pan or zoom, the side is not changed anymore to provide a stable map of the insets' positions.

input :insets I, maximum area maxA, and maximum distance maxD
output:clusters C

```
1 C \leftarrow empty \ list;
2 for inset i \in I do
       d \leftarrow maxD;
3
       closest \leftarrow NIL;
 4
       for cluster c \in C do
5
           if AreaOf (c) > maxA then
6
               continue
7
8
           end
           distance \leftarrow L2Dist(i, c);
 9
           if distance < d then
10
               closest \leftarrow c;
11
               d \leftarrow distance;
12
           end
13
       end
14
       if IsNotNil(closest) and CombinedAreaOf(i, c) \leq maxA then
15
           AddToCluster(c, i);
16
17
       end
       else AppendToList(C,CreateNewCluster(i));
18
19 end
20 return C
```

Algorithm S2: Initial clustering. AreaOf computes the area of the convex hull defined by a cluster of points. Additionally, CombinedAreaOf computes the area of the convex hull defined by a cluster that is extended by a point. L2Dist computes the Euclidean distance between an inset and the center of a cluster in pixel coordinates. Details about AddToCluster are provided in Algorithm S3.

```
input : cluster c, inset iNew
 1 d \leftarrow Infinity;
2 closest \leftarrow NIL;
3 for inset i \in C.I do
       if C.FNN = NIL then
 4
            C.FNN \leftarrow empty priority queue in descending order;
5
       end
6
       distance \leftarrow L2Dist (i, iNew);
 7
       if distance < d then
8
9
            closest \leftarrow i:
            d \leftarrow distance;
10
       end
11
12 end
13 AddToSet (C.I, i);
14 AddToQueue (C.FNN, (d, closest, iNew));
```

Algorithm S3: Add an Inset to a Cluster. In order to quickly determine breakpoints of a cluster, we are keeping track of the nearest neighbor of insets as they are being added to a cluster. Upon zooming in we then only have to evaluate if the distance of the farthest nearest neighbor is larger than the threshold and if it is we split the cluster into two separate clusters such that the first cluster contains all patterns closer to the first pattern of the pair of farthest nearest neighbors and the second cluster is composed of all the other patterns. E.g., Figure 5.5.i shows the farthest nearest neighbor pair with a black dashed line.

**input** :clusters C, zoom direction z, maximum distance maxD, maximum area maxA **output** :updated clusters C

```
1 if z == 1 then
      maxD = maxD \times 1.5;
2
      for cluster c \in C do
3
          if SizeOf (C) > 1 then
 4
              fnn \leftarrow GetFNN (C);
 5
              distance \leftarrow L2Norm (fnn);
 6
              if distance > maxD then
 7
                  [c1,c2] \leftarrow SplitClusterAt(c,fnn);
 8
                  AppendTo (C, [c1,c2]);
 9
              end
10
          end
11
      end
12
13 else if z = -1 then
      maxD = maxD \times 0.5;
14
      for cluster c1 \in C do
15
          for cluster c2 \in C do
16
              if c1 \neq c2 and L2Dist(c1, c2) < maxD and CombinedAreaOf(c1, c2) <
17
                maxA then
                  MergeClusters (c1, c2);
18
19
              end
          end
20
      end
21
```

Algorithm S4: Update clustering. Upon zooming in or out, clusters are evaluated whether they need to be split or merged. On zooming in (z == 1), split a cluster if the L2 distance of the farthest nearest neighbors (FNN) is larger than  $1.5 \times maxD$ . The FNN are defined when a point is added to a cluster. The distance between the nearest neighbor and the newly added point is stored. FNN is then defined as the pair of points on the cluster that was farthest away. Internally, FNN is a cached property of each cluster instance to quickly determine if and where a cluster would need to be split. On zooming out (z == -1), the distance between all pairs of clusters are compared. If the distance between two clusters c1 and c2 is smaller than  $0.5 \times maxD$  and the combined are is smaller than maxA the clusters are merged.

input :cluster c, importance property p
output :representative insets R

```
1 if p ≠ NIL then
2 | r1 ← GetMostImportant (C.I,p);
3 end
4 else r1 ← GetLargest (C.I);
5 ;
6 r2 ← GetClosestToCenterExcept (C.I, C.centroid, [r1]);
7 r3 ← GetFarthestFromCenterExcept (C.I, C.centroid, [r1,r2]);
8 r4 ← GetFarthestFromInsetExcept (C.I, r3, [r1,r2,r3]);
9 return [r1,r2,r3,r4]
```

Algorithm S5: Gallery Representatives. Heuristic for choosing the representative insets of an aggregated gallery inset. GetClosestToCenterExcept, GetFarthestFromCenterExcept, and GetFarthestFromInsetExcept operate in Euclidean space.